

COMPUTATIONAL MECHANICS AND OPTIMAL PROGRAMMING PARADIGM

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Abstract:

The aim of the paper is to find an optimal programming paradigm in context of the computational mechanics that is mainly focused on the numerical solution of the partial differential equations. Two paradigms - procedural and objected oriented (OOP) are compared along with a simple software development representing by a GUI. Objected oriented programming can be viewed as a good compromise among the time required for the production of the code and numerical tests procedures in the computational mechanics. Procedural programming can be suitable for a quick testing of the numerical solution of partial differential equation. If the project is extended, the code can be for reusability rebuild to classes in objected oriented programming. One computational example is shown in the paper and limitations of the selected programming paradigm are described.

Keywords:

Partial differential equations, objected oriented programming, creep curve, contact.

ACM Computing Classification System:

Applied computing → Physics

Introduction

Computational mechanics is mainly focused on the finding the approximate solution of the partial differential equations (PDE) [1]. PDEs describe natural laws mathematically and these equations are usually solved by numerical method like finite element method (FEM), finite difference method (FDM), boundary element method (BEM) etc. [1]. There is plenty of commercial and open source specialized “graphical” software like Ansys, Abaqus, Simflow, OpenFOAM, CalculiX and many more dealing with the numerical solution of PDEs (especially in the field of the continuum mechanics). Mathematical software like Mathematica, Maple or Matlab are able to handle with numerical solutions of PDEs as well. Free packages like FEniCS [2] or Code_Aster [3] are in the development and used in the various field of the continuums mechanics. Software/Toolboxes based on Matlab have also been developed [4], [5]. Once the solutions of PDE is known, the results are normally visualized in 2-D or 3-D graphs. Standardly is tested the influence of the input variables on the results. Therefore, procedural and functional programming are probably the most used in the computational mechanics. Object-oriented programming (OOP) finds in context of the computational mechanics mainly place in software development [2], [4].

According to author’s experience, it cannot be predicted whether the piece of “PDE-Testing code” will serve as a basis for the new software development or not. Hence, choosing the appropriate programming paradigm can be crucial.

The aim of the paper is to compare two programming paradigm and simple software development in the framework of Computational mechanics and in prospect of future software development. Procedural programming and OOP paradigm will be tested on the computational example; the simple software development will be expressed through the simple GUI. No exception handling or unit testing are included in the example and the Python programming language (Ver. 3.7.0) will be used.

1 Computational Example

The creep curve represents the computational example. The creep curve relates the longitudinal creepage (slip) with the tangential forces in the rolling/sliding contact [6]. Such contact situation can be found for instance between the rail and the train wheels [7], [8]. The computation is based on the equations from [6] and the input variables are listed in (Tab.1) (The underlying PDEs can be found in [9]).

Table 1. The input variables

| Variable | Unit | Notice |
|---|------|-----------------------------|
| Normal force per unit thickness (F_N) | N/mm | - |
| Friction coefficient (μ) | - | 0.5 for steel/steel contact |
| Young's modulus (E) | MPa | Material constants |
| Poissons's ratio (ν) | - | |
| Maximum contact pressure (P_{max}) | MPa | - |
| Longitudinal slip (γ) | - | %/100 |

The full-slip state is defined as:

$$\gamma^{fs} = 2(1 - \nu)\mu P_{max}/G, \quad (1)$$

where G is the shear modulus defined as:

$$G = E/2(1 - \nu). \quad (2)$$

The tangential force T is defined as:

$$T = \begin{cases} \mu F_N (1 - (1 - |\frac{\gamma}{\gamma^{fs}}|)^2) & |\gamma| < \gamma^{fs} \\ \mu F_N & |\gamma| \geq \gamma^{fs} \end{cases} \quad (3)$$

The code was written in the Scientific Python Development Environment Spyder (Ver. 3.3.1) using Python libraries numpy (Ver. 1.15.4) for numerical computation, matplotlib (Ver. 3.0.0) for graph visualisation and tkinter (Ver. 8.6) for GUI. The GUI with the given input variables is depicted in (Fig.1) and the creepage curve in (Fig.2).

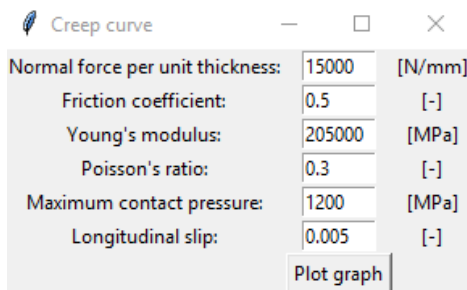


Fig.1. Simple GUI with input variables.

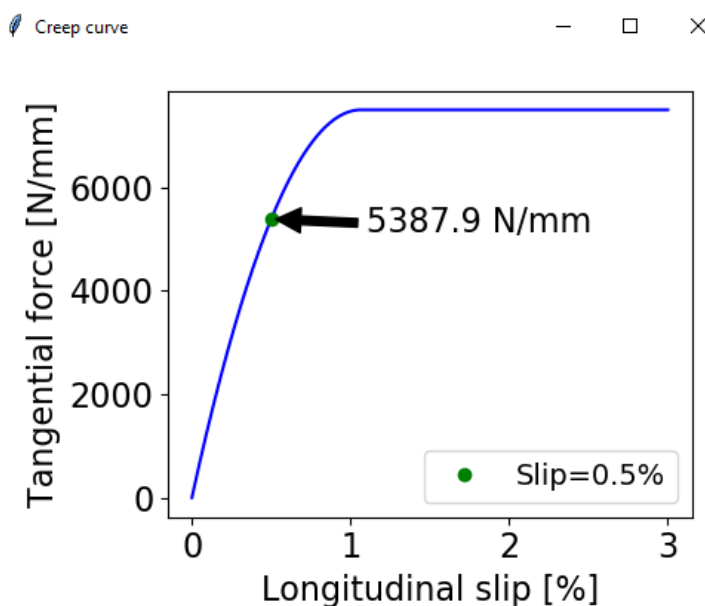


Fig.2. The creep curve – the relationship between longitudinal creepage (slip) and tangential force in rolling/sliding contact.

2 Results and Discussion

The main results are summarised in (Tab.2). Simply assuming the linear dependency between the size of the programming code and the programming time, the simple GUI requires a much more programming time than an OOP. On the other hand, the difference between the OOP and procedural programming is not pronounced.

Here has to be said that a simple GUI can probably be programmed in the more efficient way through the loop. Currently, the one entry requires a one manually written bunch of code. Nevertheless, the GUI creation generally slows down the numerical testing of the physical problem and should be left to software engineers in the next phase of the projects. OOP can be viewed in this context as a compromise between the procedural programming and possible future software development but it is not recommended for all applications.

According to author's scientific experience, OOP comes on the scene, if the developed procedure turns into a replicable entity. Otherwise, procedural programming is suitable as well. Once the piece of code is suitable for an OOP, it is still not time consuming to create a new class. Implementing known physical problem, OOP can be used from the beginning.

Table 2. Assumed linear dependency between the size of the programming code and time

| Paradigm | Size of the programming code (in lines) | Programming time (ratio to Procedural programming) |
|------------|---|--|
| Procedural | 52 | 1 |
| OOP | 61 | 1.17 |
| OOP+GUI | 157 | 3.02 |

The variety of a computational mechanics problem cannot be fully covered by two programming paradigm. Recursive programming is used as well [10], [11]. However, recursive programming technics can be implemented into the classes in the multi-paradigm language as for instance in the paper used Python.

Conclusion

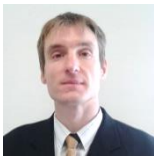
This paper tests two programming paradigm (procedural and objected oriented) along with a simple software development at one computational example in order to find an optimal paradigm suitable for an usage in the computational mechanics. The code written using objected oriented paradigm needs only a few more line than procedurally written code. The GUI slows a numerical testing of the underlying partial differential equations and should be left to the software developer in case of turning the code into a real software development. Procedural programming is suitable for a quick testing of the ideas without requirements on the reusability of the code. These two programming paradigm and functional programming are probably most used in the computational mechanics and other programming paradigms are excluded from the paper.

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